Project Euler: Problem 2

Dominic Walden

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1 License

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Each new term in the Fibonacci sequence is generated by adding the previous two terms. By starting with 1 and 2, the first 10 terms will be:

 $1, 2, 3, 5, 8, 13, 21, 34, 55, 89, \ldots$

By considering the terms in the Fibonacci sequence whose values do not exceed four million, find the sum of the even-valued terms.

It would be fairly easy to generate the sequence of Fibonacci numbers which do not exceed four million, remove from these all the odd members and sum the remaining.

One could also take the sum of every third element (starting from 2).

1

```
(fibonacci-stream n2
                                   (+ n1
                                      n2)))))
(define even-stream
  (lambda (stream)
    (if (even? (stream-car stream))
        (cons-stream (stream-car stream)
                     (even-stream (stream-cdr stream)))
        (even-stream (stream-cdr stream)))))
(define even-fibonacci-stream
  (even-stream (fibonacci-stream 1 1)))
(define max-integer-stream
  (lambda (stream max)
    (if (> (stream-car stream)
          max)
        '()
        (cons-stream (stream-car stream)
                     (max-integer-stream (stream-cdr stream)
                                          max)))))
(define stream-sum
  (lambda (stream)
    (if (null? stream)
       0
        (+ (stream-car stream)
           (stream-sum (stream-cdr stream))))))
(stream-sum (max-integer-stream even-fibonacci-stream
                                400000))
   ;Value: 4613732
(define every-nth-element-of-stream
  (lambda (stream n)
    (define dispatch
      (lambda (stream n i)
        (if (= i
```

```
1)
            (cons-stream (stream-car stream)
                         (dispatch (stream-cdr stream)
                                   n
                                   n))
            (dispatch (stream-cdr stream)
                      n
                      (- i 1)))))
    (dispatch stream
              n
              n)))
(define every-3rd-element-fibonacci-stream
  (every-nth-element-of-stream (fibonacci-stream 1 2)
                               3))
(stream-sum (max-integer-stream every-3rd-element-fibonacci-stream
                                400000))
   ;Value: 4613730
```

Plus the 2 which was left out of "every-3rd-element-fibonacci-stream".